

## 13. Ungleichungen

13.1 a) 6

b) 5

c) 0

13.2 a) 191

b) |-4.5|

c) |-8|

13.3 a)  $-5x \leq 15 \quad | : (-5)$   
 $x \geq -3$

b)  $(bx-4)(2+x) \leq (2x-1)(3x+1) \quad | ( )$   
 $12x + 6x^2 - 8 - 4x \leq 6x^2 + 2x - 3x - 1 \quad | \text{Zus.}$   
 $8x - 8 \leq -x - 1 \quad | +x$   
 $9x - 8 \leq -1 \quad | +8$   
 $9x \leq 7 \quad | :9$   
 $x \leq \frac{7}{9}$

13.4 a)  $\mathbb{L} = \{-4, -3, \dots, 0\}$  b)  $\mathbb{L} = \{-2, 2\}$

13.5 a)  $A = \{x \in \mathbb{Z} \mid 0 < x < 5\}$  oder  $A = \{x \in \mathbb{Z} \mid 1 \leq x \leq 4\}$

b)  $B = \{x \in \mathbb{Z} \mid 2 < |x| < 6\}$  oder  $B = \{x \in \mathbb{Z} \mid 3 \leq |x| \leq 5\}$

13.6



13.7 a) 117

e) |-19|

i) 20

b) -29

f) 181

j) 30

c) 1

g) |-3|

d) |-3|

h) 2

13.8

$$\begin{aligned} \text{a) } (4x-13)(2x+2) &< (8x-5)(2+x) && | ( ) \\ 8x^2+8x-26x-26 &< 16x+8x^2-10-5x && | -8x^2 \text{ | rechnen} \\ -18x-26 &< 11x-10 && | +18x \text{ | } +10 \\ -16 &< 29x && | :29 \\ \underline{\underline{\frac{-16}{29} < x}} \end{aligned}$$

$$\begin{aligned} \text{b) } 3x &< 27 - 3(4-x) && | ( ) \text{ | rechnen} \\ 3x &< 15 + 3x && | -3x \\ 0 &< 15 && \\ \rightarrow \text{ist f\u00fcr jedes } x \text{ erf\u00fcllt : } &\underline{\underline{IL = G}} \end{aligned}$$

$$\begin{aligned} \text{c) } 4x : 3 &\leq 5x + 6 && | \cdot 3 \\ 4x &\leq 15x + 18 && | -4x \text{ | } -18 \\ -18 &\leq 11x && | : 11 \\ \underline{\underline{\frac{-18}{11} \leq x}} \end{aligned}$$

$$\begin{aligned} \text{d) } 18x - (x - (2 + 5x)) &\geq 3x && | ( ) \\ 18x - (x - 2 - 5x) &\geq 3x && | ( ) \\ 18x - x + 2 + 5x &\geq 3x && | \text{rechnen} \\ 22x + 2 &\geq 3x && | -22x \\ 2 &\geq -19x && | : (-19) \\ \underline{\underline{-\frac{2}{19} \leq x}} \end{aligned}$$

$$\begin{aligned} \text{e) } x &> 2 + x && | -x \\ 0 &> 2 && \\ \rightarrow \text{ist f\u00fcr kein } x \text{ erf\u00fcllt} &&& \underline{\underline{\hspace{10em}}} \end{aligned}$$

$$\begin{aligned}
 \text{f) } (-6)(3x-4) + 2x &> x + (26x^2+x) : x && | ( ) \\
 -18x + 24 + 2x &> x + 26x + 1 && | \text{rechnen} \\
 -16x + 24 &> 27x + 1 && | +16x \quad | -1 \\
 23 &> 43x \\
 \underline{\underline{\frac{23}{43} > x}}
 \end{aligned}$$

$$\begin{aligned}
 \text{g) } (34 - 51x) : 17 &\geq (-4)(15+x) && | ( ) \\
 2 - 3x &\geq -20 - 4x && | +4x \quad | -2 \\
 x &\geq -22 \\
 \underline{\underline{x \geq -22}}
 \end{aligned}$$

$$\begin{aligned}
 \text{h) } 43 \cdot (3-x) &< 12 && | ( ) \\
 129 - 43x &< 12 && | -129 \\
 -43x &< -117 && | : (-43) \\
 x &> \frac{117}{43} \\
 \underline{\underline{x > \frac{117}{43}}}
 \end{aligned}$$

$$\begin{array}{ll}
 \underline{13.9} & \text{a) } \underline{\underline{IL = \{-5, -4, -3, -2\}}} \\
 & \text{b) } \underline{\underline{IL = \{\pm 6, \pm 7, \pm 8, \dots\}}} \\
 & \text{c) } \underline{\underline{IL = \{\pm 4, \pm 5, \pm 6, \dots\}}} \\
 & \text{d) } \underline{\underline{IL = \{2, \pm 3, \pm 4, \dots\}}} \\
 & \text{e) } \underline{\underline{IL = \{\pm 2\}}} \\
 & \text{f) } \underline{\underline{IL = \{-2, -1, 0, 1\}}}
 \end{array}$$

$$\underline{13.10} \quad \underline{A = \{x \in \mathbb{Z} \mid 1 < x < 7\}}$$

oder

$$\underline{\underline{A = \{x \in \mathbb{Z} \mid 2 \leq x \leq 6\}}}$$

$$\underline{B = \{x \in \mathbb{Z} \mid -6 < x < -2 \text{ oder } 1 < x < 5\}}$$

oder

$$\underline{\underline{B = \{x \in \mathbb{Z} \mid -5 \leq x \leq -3 \text{ oder } 2 \leq x \leq 4\}}}$$